Due date: Friday February 3, 12:00 noon; lates until Monday Feb 6, 12:00 noon (-25\%).
Objectives: Prolog programming practice! All questions use Sicstus Prolog interpreter. (SWI Prolog and others should work too, with some modifications). For programming questions, hand in a source listing as well as a dialog listing (eg. use the 'script' utility of unix).

1. (a) Construct Prolog rules defining the following family relations:

| mother | father | son |
| :--- | :--- | :--- |
| daughter | child_of | grandmother |
| grandfather | grandson | granddaughter |
| grandchild | aunt | uncle |
| niece | nephew | cousin |
| second-cousin* | sibling | great-grandparent |

(* more complicated than you might think -- see Wikipedia page!)
(b) Add to the database information about your own family tree, and run some queries to test the different predicates. Make sure a person is not his or her own sibling!
2. Write a Prolog program that solves the following arithmetic puzzle. The 16 empty squares represent the integers 1 through 16, with no repeats. No value is used more than once. The first row represents the condition,

$$
(A+B-C) / D=9
$$

Your program should report the solution integers in row-major order (row 1, row 2, etc.). With backtracking, your program should report multiple solutions of the puzzle if they exist. (Note: in Sicstus, the " $/$ " operator always returns floats, while "//" returns integers).

3. (a) Take the attached code from Clocksin and Mellish which does symbolic differentiation, type it into Prolog, and try it on some example expressions.
(b) Write a new predicate simplify(Old, New). Old is an arithmetic expression as generated by the symbolic differentiation routine in (a). New is a simplified expression. The types of simplifying transformations can look as follows:

$$
\begin{aligned}
& E+0 \rightarrow E \\
& E * 0 \rightarrow 0 \\
& E-E \rightarrow 0 \\
& E+E \rightarrow 2 * E \\
& E / 1 \rightarrow E \\
& \text { etc. }
\end{aligned}
$$

Think of a reasonable number of simplifying transformations, and implement them. You can test simplify/2 without using the differentiation routine. In general, you will have better results with your simplifier if you recursively simplify arguments before the parent expression. For example,

$$
\begin{aligned}
5^{\star}((2 \star 3)-(2 * 3)) & \rightarrow 5^{\star 0} 0 & & \text { (using "E-E") } \\
& \rightarrow 0 & & \text { (using E*0) }
\end{aligned}
$$

