

### Interior of Triangle Example

Given fast signed distance of point-to-line formula:

$$\text{dist}(P_a, P_b, P) = Ax + By + C$$

where:  $A = (y_0 - y_1)$

$B = (x_1 - x_0)$

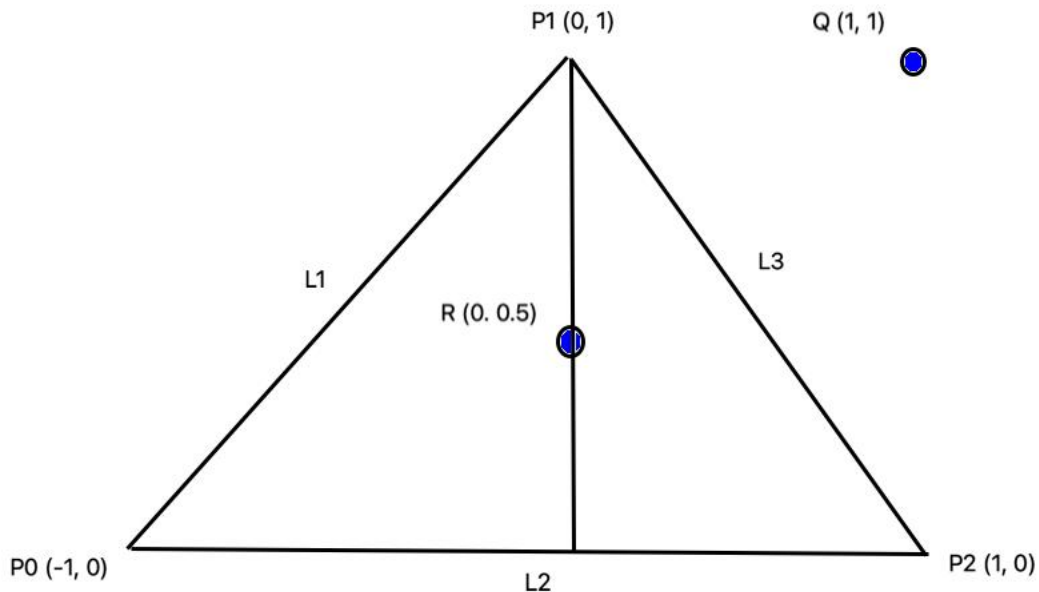
$C = x_1y_1 - x_1y_0$

$P_a = (x_0, y_0),$

$P_b = (x_1, y_1)$

and  $P = (x, y)$

Here,  $P_a$  and  $P_b$  are 2 points on an edge of triangle (for example, vertices), and  $P$  is a point on the plane. We wish to test if  $P$  is inside or outside the triangle.



In the above illustration, testing point  $Q$ :

$$\text{dist}(P_1, P_0, Q) = -1$$

$$\text{dist}(P_2, P_1, Q) = 1$$

$$\text{dist}(P_0, P_2, Q) = -1$$

Since signs change, then  $Q$  is outside of triangle (could have stopped after second call to dist).

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On the other hand, for point R:

$$\text{dist}(P1, P0, R) = -0.5$$

$$\text{dist}(P2, P1, R) = -0.5$$

$$\text{dist}(P0, P2, R) = -1$$

Since the signs are the same, R is in the interior of the triangle.